

Atomic Clocks and Frequency Standards

The Battel for Exactness

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① Time and Frequency Measurement through the years

② Atomic Clock Concept

③ Microwave Frequency Standards

④ Outlook

Importance of (correct) Time Measurement



<http://ageofsail.wordpress.com/>

Importance of Time Measurement - Today



<http://wikipedia.org/>

Clocks & Frequency Standards

- fundamental importance time measurement
- challenge - man made clocks

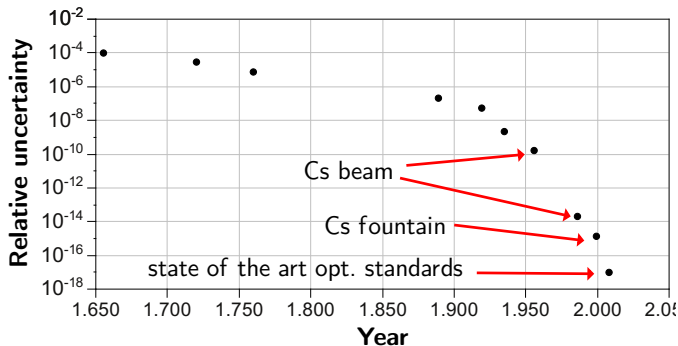


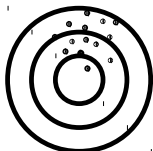
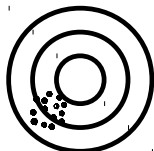
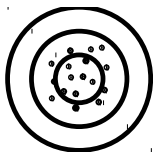
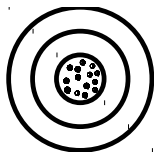
Figure: development clocks, partially after [1]

[1] F. Riehle, *Frequency Standards*, Wiley, 1st ed. 2004

Requirements Frequency Standard

- clock: basis frequency standard with frequency ν_0 measure amount of oscillation cycles, time T

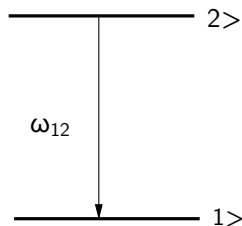
$$T = n \cdot \frac{1}{\nu_0}$$



- precise/stable, accurate frequency (short-, longterm stability)
- reproducibility
- frequencies in absolute unit in comparison to other standards
 - intrinsic - primary standards
 - calibration - back tracking

Clocks & Frequency Standards

- atomic clocks transition in microscopic quantum systems
- new SI definition of time unit in 1967: caesium primary standard



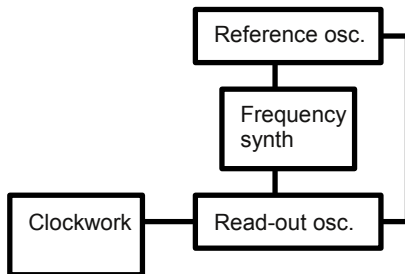
Definition

"The second is the duration of 9 192 631 770 periods of the radiation corresponding to the transition between the two hyperfine levels of the ground state of the caesium 133 atom." [2]

[2] *Comptes Rendus de la 13^e CGPM* (1967/68), 1969, 103

Atomic Clock Concept

- 2 separated oscillators
- one isolated reference, other read-out link

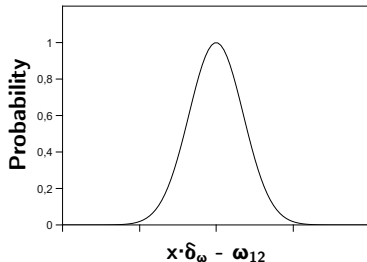
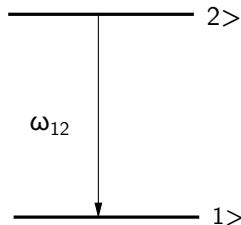


- reference oscillator quantum system
- read-out oscillator quartz crystal (piezoelectric)

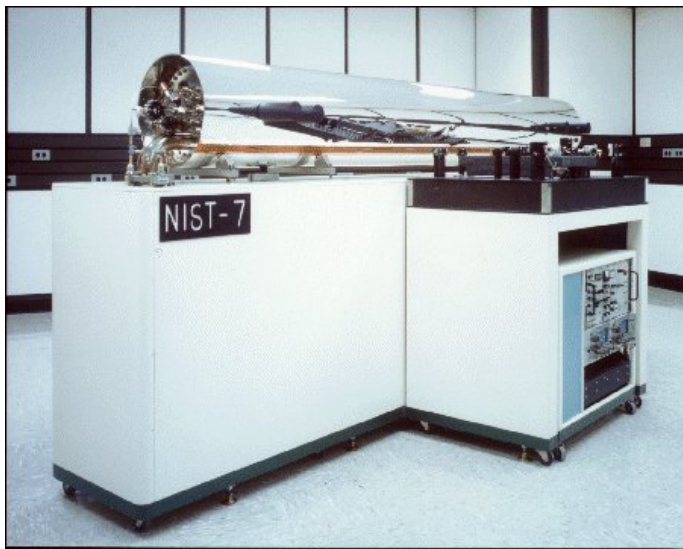
Atomic Clock Concept

quantum system, two level system states $|1\rangle$, $|2\rangle$

- 1 preparation one of the states
- 2 interaction with electromagnetic field
- 3 measure probability for transition
- 4 lock read-out oscillator on frequency of probability maximum



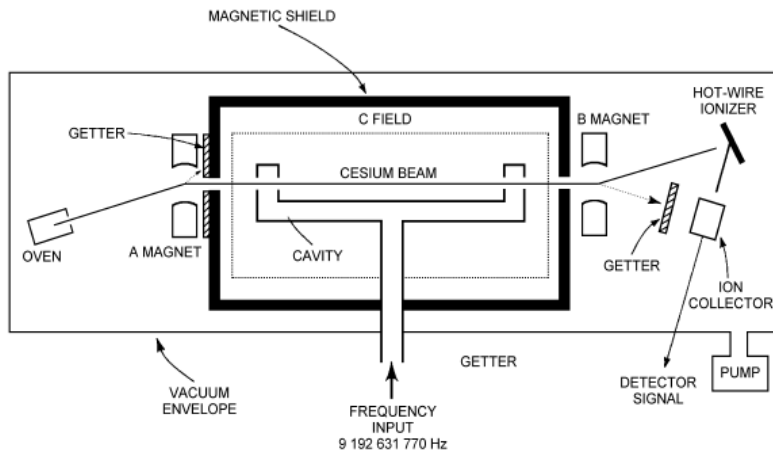
^{133}Cs Clocks - Beam clocks



<http://www.nist.gov/>

^{133}Cs Clocks - Beam clocks

- especial frequency standard
- basic setup NIST (from [5] D. Sullivan, J. Res. Natl. Inst. Stand. Technol. **106**, 2001)



^{133}Cs Clocks - Beam clocks

- ^{133}Cs :

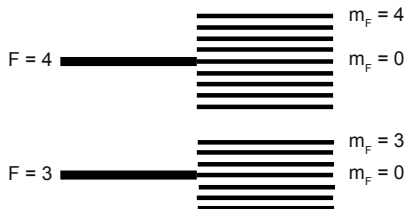
nuclear spin $I = 7/2$

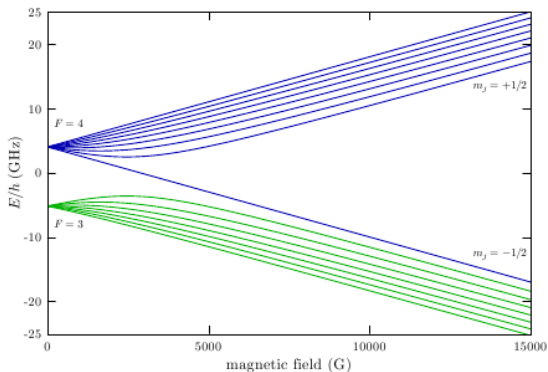
total spin $J = 1/2$

\Rightarrow hyperfine structure, states $F = I \pm J = 3, 4$

- transition $|F = 4, m_F = 0\rangle \rightarrow |F = 3, m_F = 0\rangle$: $\Delta\nu = 919263770$ Hz
(@ zero magnetic field)

- Zeeman split





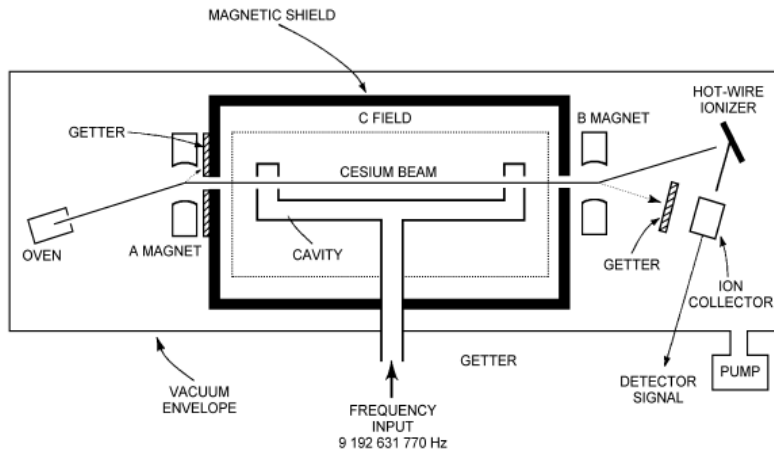
Zeeman split in external magnetic field

inhomogeneous field:

$$\vec{F} = -\mu_{\text{eff}} \nabla \vec{B}$$

[6] Daniel A. Steck, "*Cesium D Line Data*," (revision 2.1.2, 12 August 2009)

^{133}Cs Clocks - Beam clocks



Aim

$$\text{Interest in high } Q = \frac{\omega_0}{\Delta\omega}$$

Broadening processes:

- natural lifetime τ_I : $\Delta\omega_I \propto \frac{1}{\tau_I}$
 \Rightarrow negligible i.e. ^{133}Cs stable
- Doppler broadening
from energy, momentum conservation
+ absorption, - emission, relativistic calculation

$$\Rightarrow \hbar\omega = \hbar\omega_{12} + \hbar\vec{v}_{1,2} \cdot \vec{k} \pm \frac{(\hbar\omega)^2}{2m_0c^2} - \hbar\omega_{12} \frac{v_{1,2}^2}{2c^2} + \dots$$

Challenges - Broadening Processes

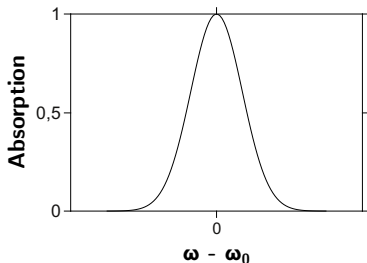
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2nd term first-order Doppler effect \Rightarrow Gaussian broadening

$$FWHM = \omega_{12} \sqrt{2 \ln 2 \frac{k_B T}{mc^2}}$$

3rd term recoil effect

4th term second-order Doppler effect



\Rightarrow avoided by low temperature regime

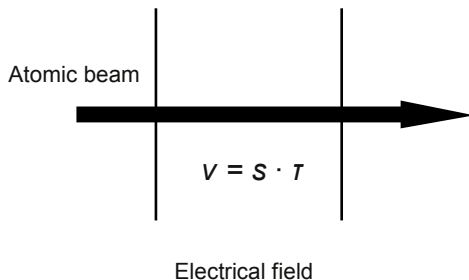
Challenges - Broadening Processes

- Collision broadening: $\Delta\omega_{\text{col}} \propto \frac{1}{\tau_{\text{col}}} \propto p \Rightarrow$ pressure reduction
- Intersection Time broadening

important contribution to the linewidth broadening

$$\Delta\omega_{\text{it}} \propto \frac{1}{\tau_{\text{it}}}$$

solution enhancement τ_{it}



- How slow an atomic beam can be made?
- Homogeneity of the electromagnetic field?

⇒ concept Ramsey spectroscopy (Nobel prize 1989)

Rabi Flopping

- atomic beam *one* interaction
- two level system

⇒ solution: oscillating occupation probability

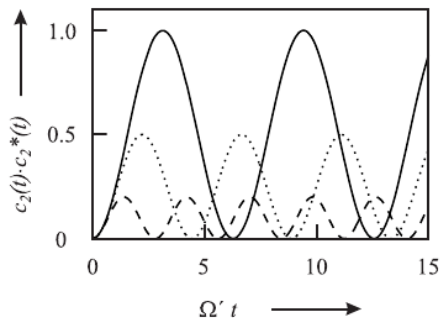


Figure: from [1] F. Riehle, *Frequency Standards*

- excited state $|2\rangle$:

$$p_2(t) = \frac{\Omega_R}{\Omega'_R} \sin^2 \frac{\Omega'_R t}{2}$$
$$\Omega'^2_R = \Omega^2_R + \Delta\omega^2$$

Ω_R : Rabi frequency

- amplitude decrease with $\Delta\omega$

Ramsey Spectroscopy

- idea two separated interactions time τ and between no field in between for time T

⇒ probability for transition interference pattern

- near resonance $|1\rangle \rightarrow |2\rangle$

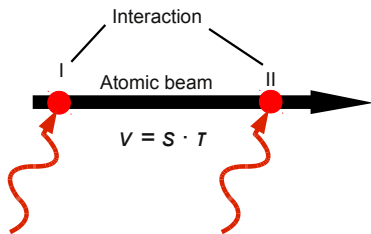
$$p(\tau + T + \tau) \simeq \frac{1}{2} \sin^2 \Omega_R \tau (1 + \cos 2\pi(\nu - \nu_{12})T)$$

$$\Rightarrow FWHM = \frac{1}{2T}$$

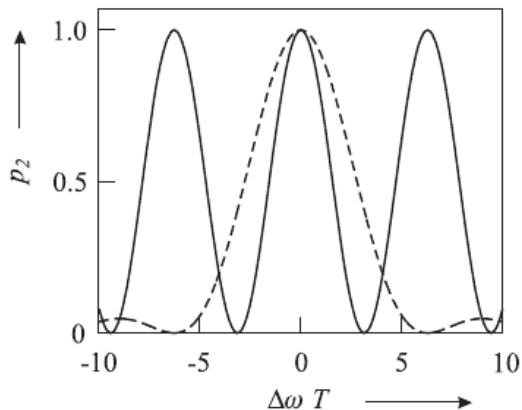
maximum for $\Omega_R \tau = \frac{\pi}{2} \rightarrow \pi/2$ pulses

[3] M. Ramsey, Phys. Rev. **78** (6), 1950

[1] F. Riehle, *Frequency Standards*



Ramsey Spectroscopy



- enhancement signal linewidth
- amplitude, period nearly unaffected

[1] F. Riehle, *Frequency Standards*

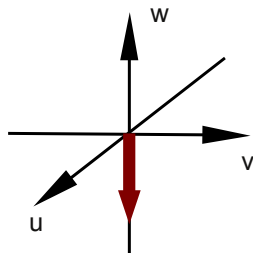
Ramsey Spectroscopy - pseudo spin picture

density matrix ρ_{11} ρ_{22} probability state $|1\rangle$ $|2\rangle$:

$$\rho = \begin{pmatrix} \rho_{11} & \rho_{12} \\ \rho_{21} & \rho_{22} \end{pmatrix}$$

Optical Bloch equations (with $\tilde{\rho}_{12} \equiv e^{-i\delta t} \rho_{12}$, $\tilde{\rho}_{21} \equiv e^{+i\delta t} \rho_{21}$):

$$\begin{pmatrix} u \\ v \\ w \end{pmatrix} = \begin{pmatrix} \tilde{\rho}_{21} + \tilde{\rho}_{12} \\ i(\tilde{\rho}_{21} - \tilde{\rho}_{12}) \\ \rho_{22} - \rho_{11} \end{pmatrix}$$
$$\frac{d}{dt} \begin{pmatrix} u \\ v \\ w \end{pmatrix} = \begin{pmatrix} \Omega_R \\ 0 \\ \delta \end{pmatrix} \times \begin{pmatrix} u \\ v \\ w \end{pmatrix}$$



*) i.e. P. Meystre and M. Sargent, *Elements of Quantum Optics*

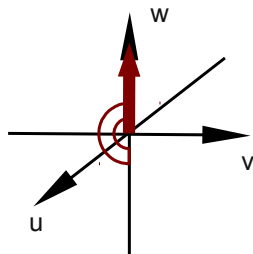
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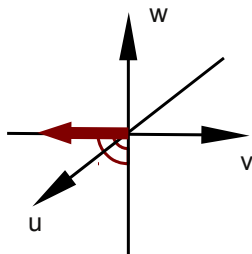
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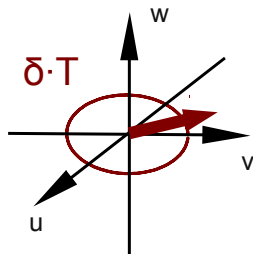
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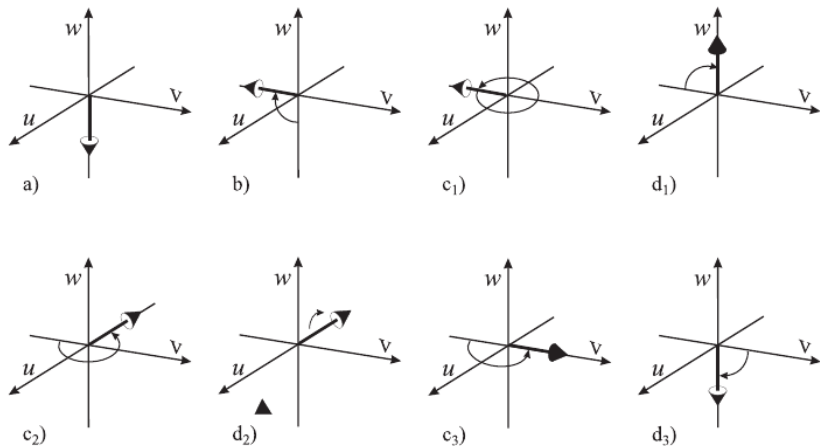
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Ramsey Spectroscopy - pseudo spin picture



from [1] F. Riehle, *Frequency Standards*

Ramsey Spectroscopy - pseudo spin picture

interference pattern

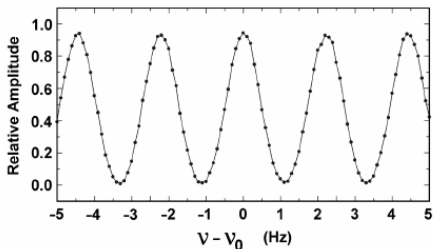
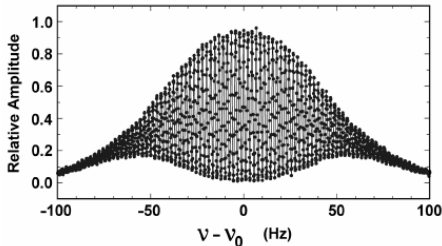
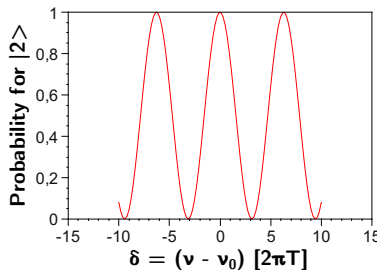
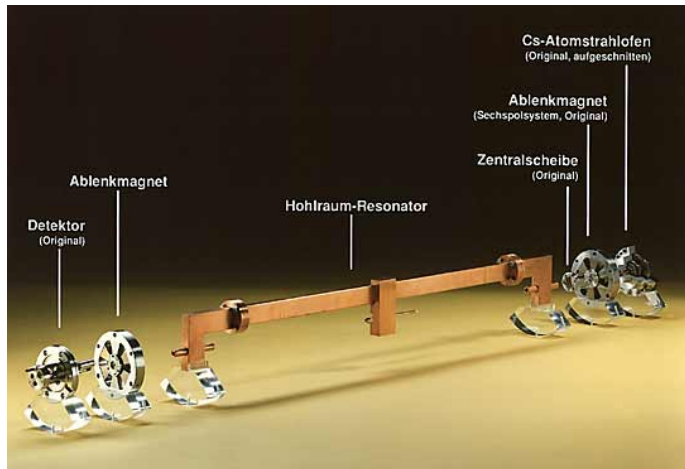


Figure: from [5] D. Sullivan, J. Res. Natl. Inst. Stand. Technol. **106**, 2001

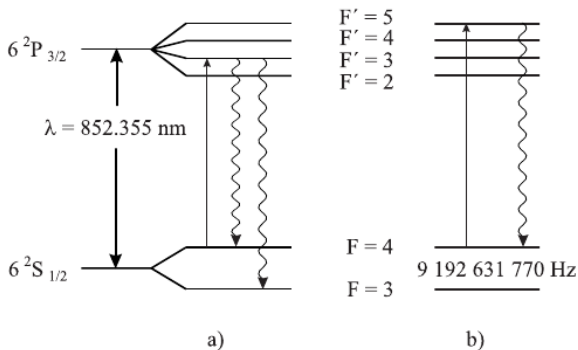
^{133}Cs Clocks - Beam clocks



<http://www.ptb.de/>

^{133}Cs Clocks - Beam clocks, optical pumping

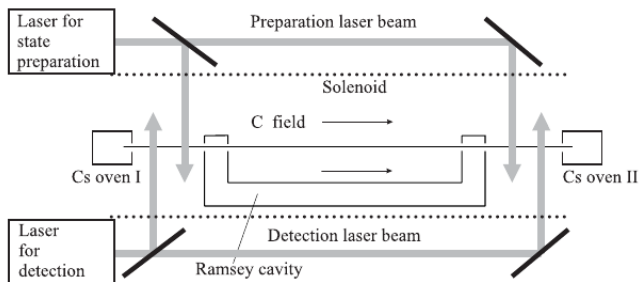
- enhance signal to noise ratio
- optical pumping for state selection
- detection optical transition



- a) pumping, b) detection fluorescence photons

from [1] F. Riehle, *Frequency Standards*

- basic layout



from [1] F. Riehle, *Frequency Standards*

- challenge cavity:

$$\text{length } (\Delta\nu = 1/2T)$$

versus

additional phase shift due to manufacturing limits

relative uncertainty:

- NIST: NIST-7: 4.4×10^{-15}
- PTB: CS1: 8×10^{-15}

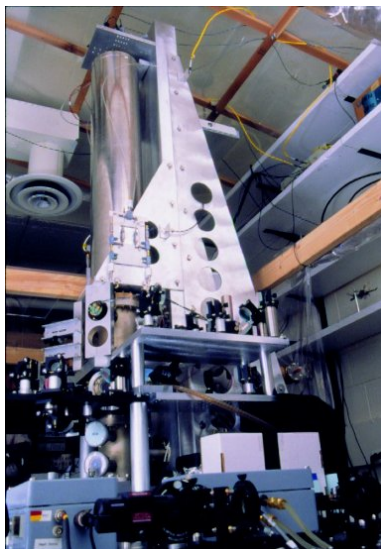
[5] D. Sullivan, *et al*, J. Res. Natl. Inst. Stand. Technol. **106**, 2001

[7] A. Bauch, **42** (2005), Metrologia **42**, 2001

^{133}Cs Clocks - fountain clocks

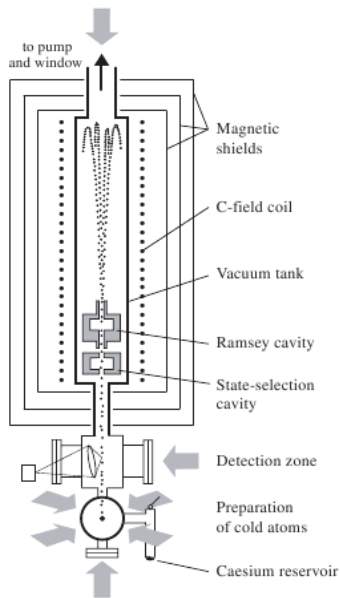
One step further!

- laser cooled atomic clocks
- two approaches:
 - enhance T
 - reduce phase shift from cavity
- fountain design



<http://www.nist.gov/>

^{133}Cs Clocks - fountain clocks

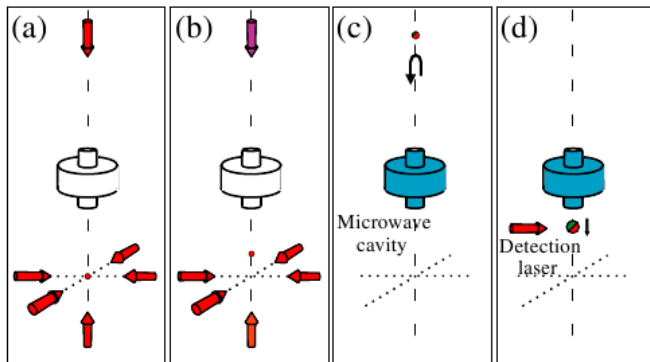


- two interactions $\pi/2$ -pulses (Ramsey)
- one cavity
 \Rightarrow reduced phase shift
- laser cooled atoms $2 \mu\text{K}$, enhanced T

[8] R. Wynands *et al*, Metrologia **42**, 2005

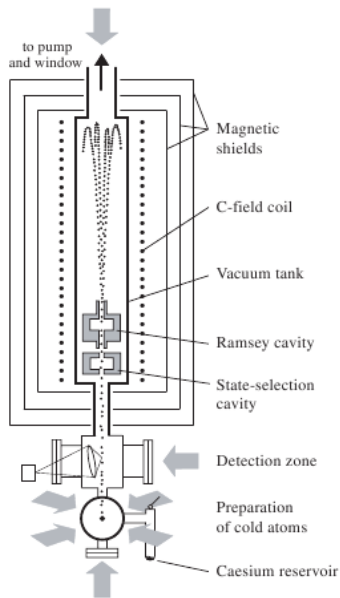
^{133}Cs Clocks - fountain clocks

process



[8] R. Wynands *et al*, *Metrologia* **42**, 2005

^{133}Cs Clocks - fountain clocks



- cold atoms - Magneto Optical Trap or Optical Molasse

- lifting atoms with $c\delta_\nu/\nu_{12}$ for

$$\text{laser upwards: } \nu = \nu_{12} + \delta_\nu$$

$$\text{laser downwards: } \nu = \nu_{12} - \delta_\nu$$

- state selection:

$$\text{from cooling in } |F = 4, m_F\rangle$$

$$\pi\text{-pulse } |F = 4, m_F = 0\rangle \rightarrow |F = 3, m_F = 0\rangle$$

"laser-pushing" other states

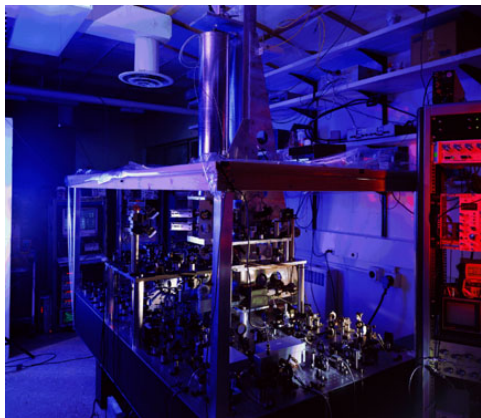
$$|F = 4, m_F\rangle \rightarrow |F' = 5, m_F\rangle$$

[8] R. Wynands *et al*, Metrologia **42**, 2005

^{133}Cs Clocks - fountain clocks, performance

- today's measurement standard
PTB: CSF2 2009
- relative uncertainties:

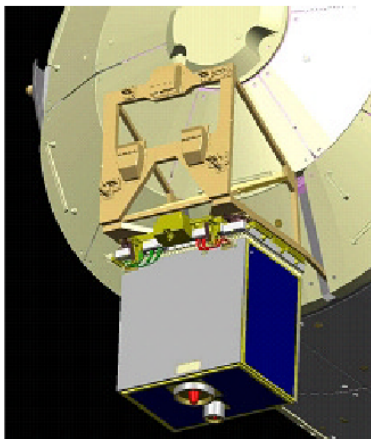
PTB CSF2: 0.8×10^{-15}
NIST NIST-F1: 1×10^{-15}
(0.5×10^{-15})



<http://www.nist.gov/>

remaining problems:

- cold collision shift
 - ⇒ density reduction
 - increased statistical noise
 - ⇒ other atomic species ^{87}Rb
- increasing flight time
 - not possible on earth
 - ⇒ experiments in micro gravity



<http://www.esa.int/>











- 2001 PHARO project
- 2010 ISS module ACES
uncertainty $\sim 10^{-16}$ regime

<http://www.dlr.de/>

- next generation on earth optical frequency standards for atomic clocks
- uncertainty $< 10^{-17}$ regime

Bibliography

-  [1] F. Riehle, *Frequency Standards*, Wiley, 1st ed. 2004
-  [2] *Comptes Rendus de la 13^e CGPM (1967/68)*, 1969, 103
-  [3] M. Ramsey, *A Molecular Beam Method with Separated Oscillating Fields*, Phys. Rev. **78** (6), 1950
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-  [6] Daniel A. Steck, "*Cesium D Line Data*," available online at <http://steck.us/alkalidata> (revision 2.1.2, 12 August 2009)
-  [7] A. Bauch, *The PTB primary clocks CS1 and CS2* Metrologia **42**, 2005, J. Res. Natl. Inst. Stand. Technol.**106**, 2001
-  [8] R. Wynands *et al*, *Atomic fountain clocks* ,Metrologia **42**, 2005