

Astroparticle Physics

- an introduction with a focus on galactic cosmic rays

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Über Beobachtungen der durchdringenden Strahlung bei sieben Freiballonfahrten

Von V. F. Hess

(Physik. Zeitschr. **14**, 1084, 1912)

[...]

Die Ergebnisse der vorliegenden Beobachtungen scheinen am ehesten durch die Annahme erklärt werden zu können, daß eine eine Strahlung von sehr hoher Durchdringungskraft von oben her in unsere Atmosphäre eindringt und auch noch in den untersten Schichten einen Teil der in geschlossenen Gefäßen beobachteten Ionisation hervorruft.

[...]

The fifth ballon flight



1 Introduction

Cosmic rays is all radiation consisting of charged relativistic particles impinging on the Earth' atmosphere

High energy cosmic rays: $E > 1 \text{ GeV}$

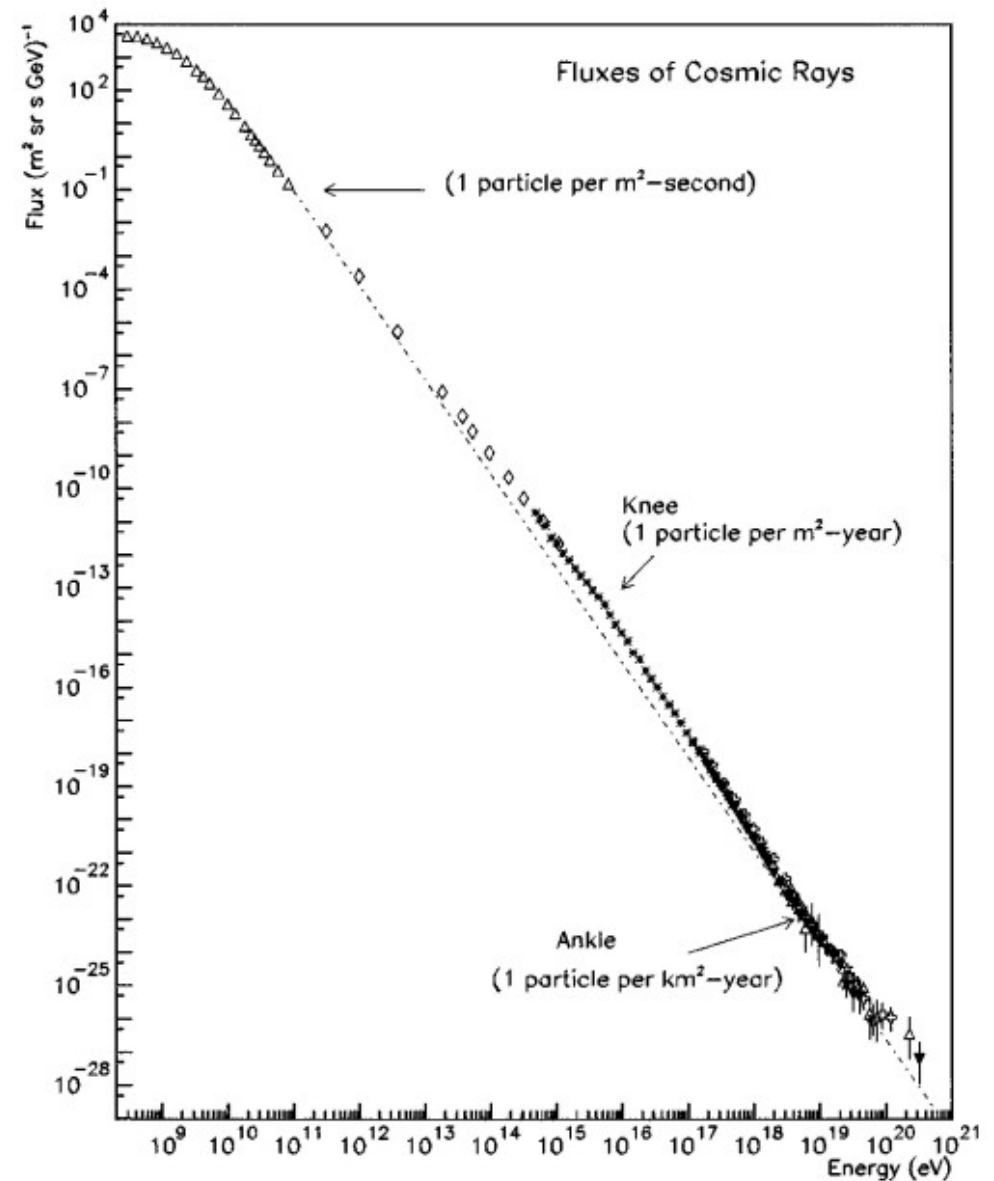
Gamma-ray and neutrinos

- created as secondaries of high energy cosmic rays
- help to learn more about cosmic rays and their sources (“multi-messenger”)

Cosmic Ray Spectrum

- nearly featureless
- extending over eleven orders of magnitude from a few GeV to a few $\cdot 10^{20}$ eV

Many more known (later)



Historical Remarks

- 1912 Victor Hess discovered cosmic rays
- 1929 Skobelzyn observed first cosmic ray in cloud chamber; Bothe & Kohlhörster showed that tracks are curved in a magnetic field
- 1928 Clay observed latitude effect
- 1932 Anderson discovered the positron in cosmic rays
- 1932 Raged debate in USA about sources of cosmic rays
- 1934 The sign of the east-west asymmetry showed that cosmic rays are positively charged
- 1934/1938 Rossi and Auger discovered extensive air showers
- 1934 Bethe and Heitler developed the electromagnetic cascade theory
- 1949 Fermi proposed that cosmic rays are accelerated by bouncing off magnetic clouds
- 1952/1954 First human accelerator reaching $p > 1$ GeV
- 1972 Launch of the SAS-2 satellite marked the start of high energy gamma-ray astronomy
- 1976 Start of the first prototype of a large scale underwater detector for high energy neutrino astronomy, DUMAND, in Hawaii
- 1989 First detection of the Crab Nebula in very high energy gamma-rays ($E > 100$ GeV)
- 1998 Superkamiokande found first convincing evidence for massive neutrinos
- ...

Aspects of Cosmic Ray Physics

- Astrophysical aspects
 - What are the sources?
 - How do they accelerate cosmic rays?
 - What happens during the journey of cosmic rays to Earth?
- Interactions of particles in the atmosphere
- Experimental methods to detect cosmic rays, gamma rays, neutrinos
- Connections between cosmic ray physics and searches for physics beyond the Standard Model

Our Milky Way



Our Milky Way

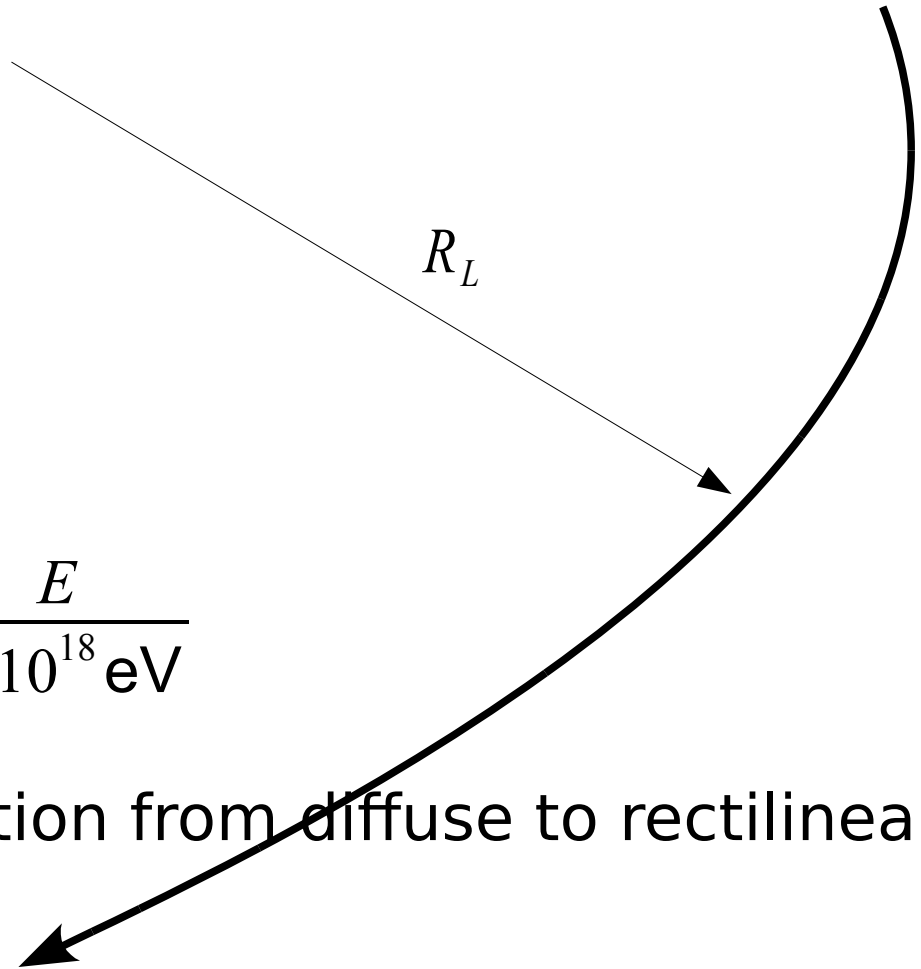
- Average magnetic field

$$B = 3 \mu\text{G}$$

- Larmor radius

$$R_L = \frac{c p}{z e B} \approx 100 \text{ pc} \frac{3 \mu\text{G}}{B} \frac{E}{Z \cdot 10^{18} \text{ eV}}$$

- $E = 10^{18} \text{ eV}$ marks the transition from diffuse to rectilinear propagation of cosmic rays



Basic notation of particle physics – a reminder

- **Optical/interaction depth**

$$\frac{N \sigma}{A} = n l \sigma = \tau = \text{optical depth}$$

- **Absorption**

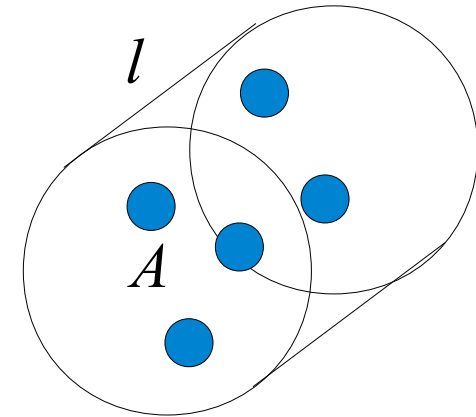
$$dI = -I d\tau = -I n \sigma dl$$

$$I = I_0 \exp(-\tau) \quad \text{or} \quad I(l) = I_0 \exp\left(-\int_0^l dl n \sigma\right)$$

- **Slant depth**

$$X(l) = \int_0^l dl' \rho(l')$$

measures the weight per area of the material crossed



Galactic Cosmic Rays – Basic observations

- Integral intensity $I(>E) = \int_E^{\infty} dE' I(E')$

- Flux $\Phi = \int d\Omega I(E) \cos\theta = I(E) \int_0^{2\pi} d\phi \int_0^{\pi/2} d\theta \sin\theta \cos\theta$
 $= \pi I(E) \int_0^{\pi/2} d\theta \sin 2\theta = \pi I(E)$

for isotropic intensity

- (differential) number density of particles with velocity v

$$n(E) = \frac{4\pi}{v} I(E)$$

More general

$$I = \frac{d^4 N}{d A dt d \Omega d E}$$

$$d N = f(\vec{x}, \vec{p}) d^3 x d^3 p$$

with $f(\vec{x}, \vec{p}) =$ phase space distribution

$$\Rightarrow I(\vec{x}, p, \theta, \phi) = v p^2 \frac{dp}{dE} f(\vec{x}, \vec{p}) = p^2 f(\vec{x}, \vec{p})$$

Abundances

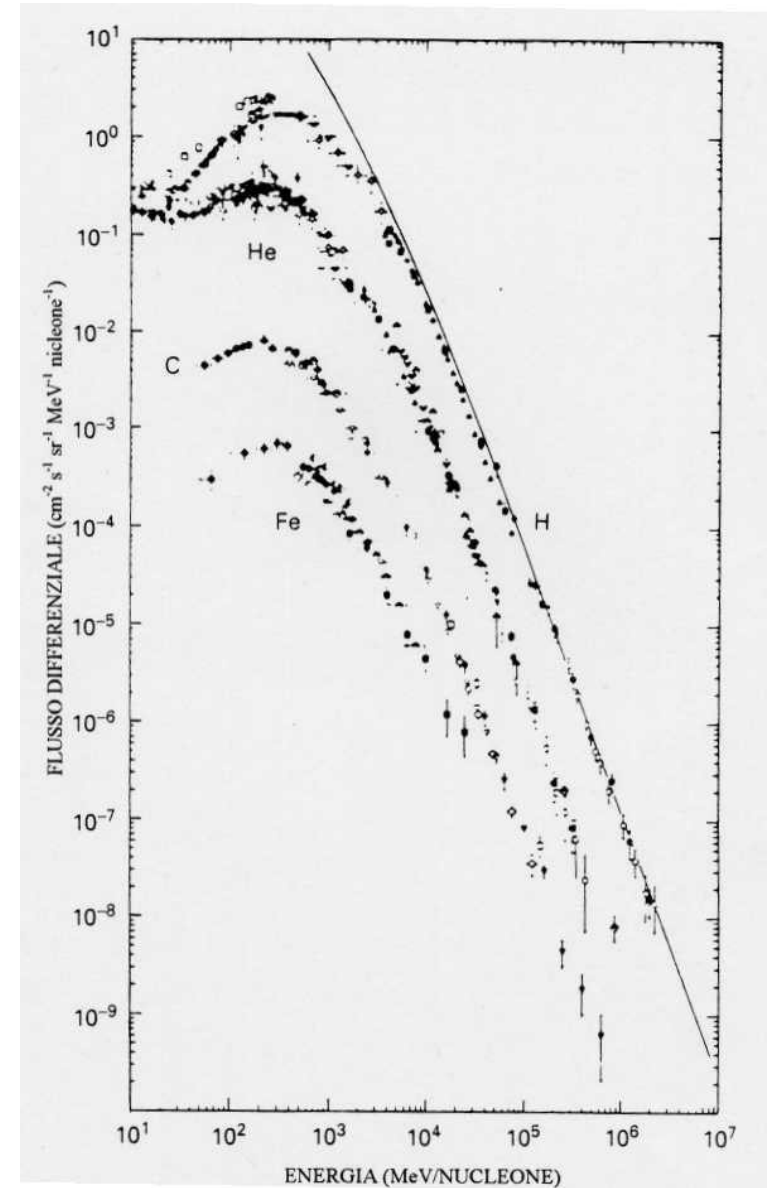
- Nuclei 98%
- Electrons 1%

Nuclei

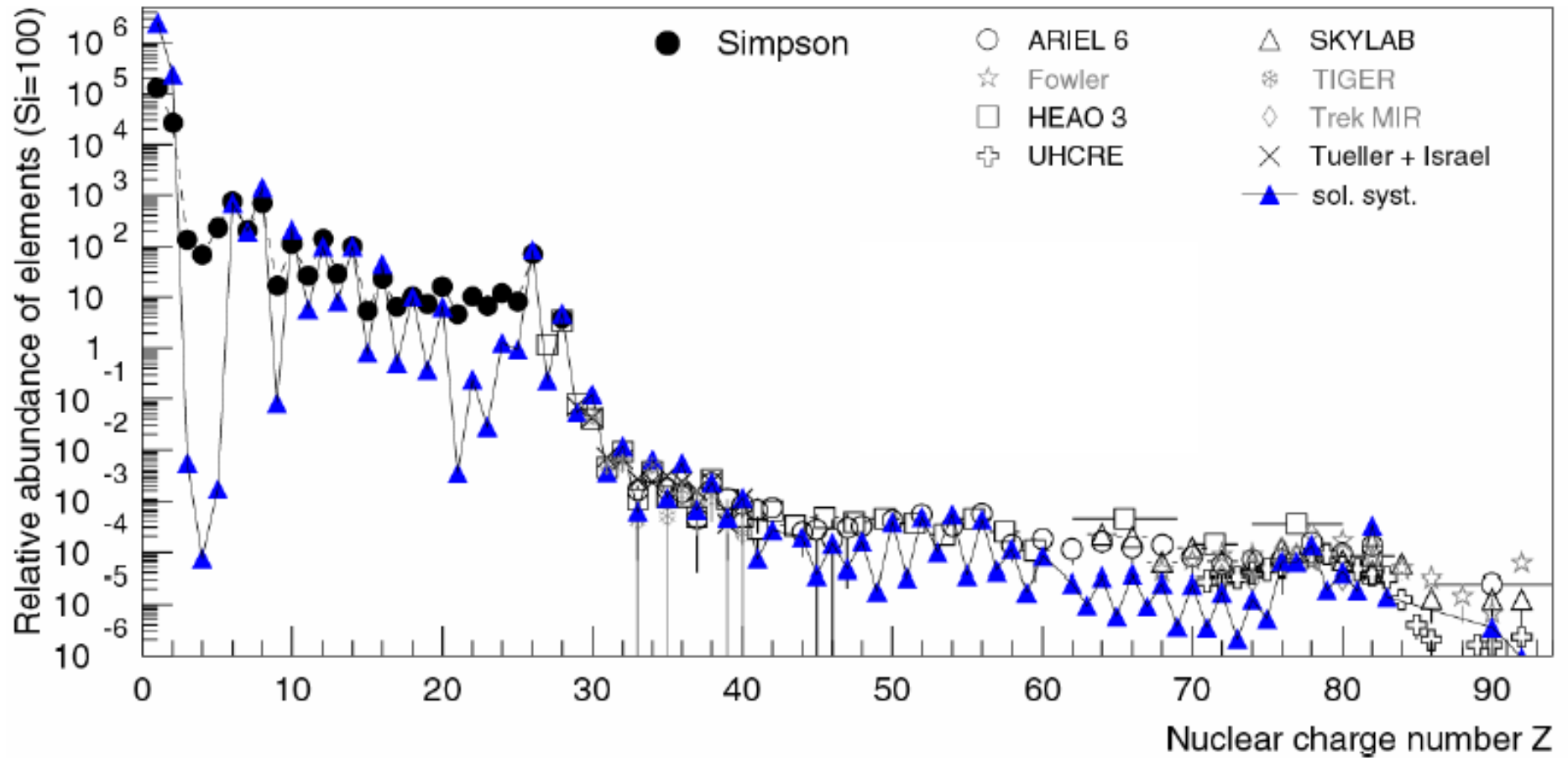
- Protons 87%
- He 12%
- heavier nuclei ~1%

Above a few GeV

$$I(E) \sim 1.8 E^{-\alpha} \frac{\text{particles}}{\text{cm}^2 \text{ s sr GeV}}$$



Abundances



measured ratio $\frac{n_{LiBeB}}{n_{CNO}} \approx 0.25$

Cascade equation for two species of particles

$$\frac{d n_p}{d X} = -\frac{n_p}{\lambda_p} \text{ and } \frac{d n_s}{d X} = -\frac{n_s}{\lambda_s} + p_{sp} \frac{n_p}{\lambda_p}$$

$X = \int dl \rho(l)$ measures the amount of transversed matter

$\lambda_i = m/\sigma_i$ interaction lengths (in gr/cm^2)

$p_{sp} = \sigma_{sp}/\sigma_{tot}$ spallation probability

Solution $\frac{n_s}{n_p} = p_{sp} \frac{\lambda_s}{\lambda_s - \lambda_p} \left[\exp\left(\frac{X}{\lambda_p} - \frac{X}{\lambda_s}\right) - 1 \right]$ for $n_s(0) = 0$

$$\frac{n_s}{n_p} = p_{sp} \frac{\lambda_s}{\lambda_s - \lambda_p} \left[\exp\left(\frac{X}{\lambda_p} - \frac{X}{\lambda_s}\right) - 1 \right]$$

$s = \text{LiBeB}$ with $\lambda_s \approx 10 \text{ g/cm}^2$

$p = \text{CNO}$ with $\lambda_p \approx 6.7 \text{ g/cm}^2$ and $p_{sp} = \frac{\sigma_{sp}}{\sigma_{tot}} \approx 0.35$

$$\left(\frac{n_s}{n_p} \right)_{meas} \approx 0.25$$

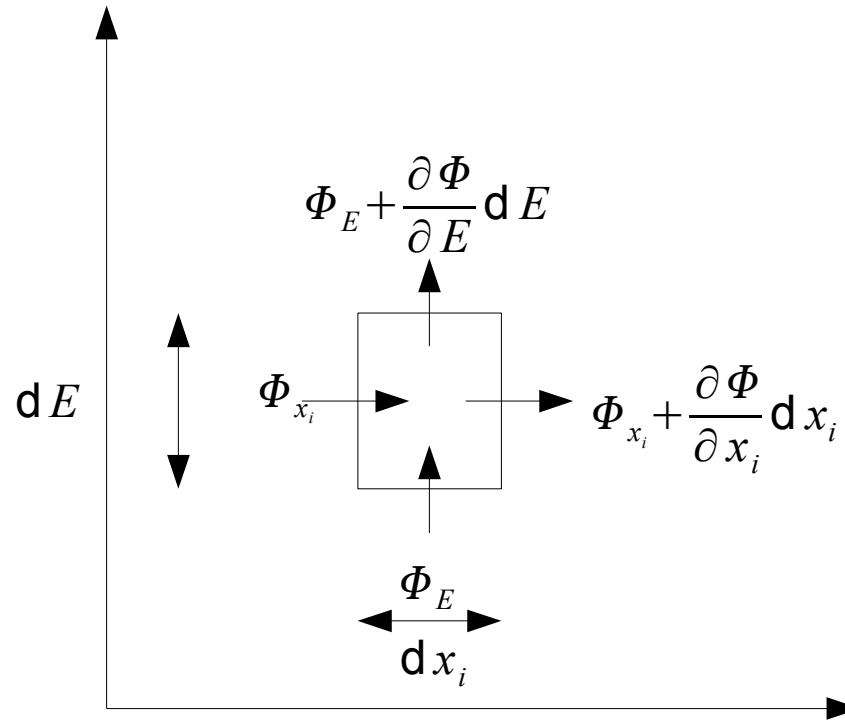
\Rightarrow fits for $X \approx 0.56 \text{ g/cm}^2$

Slant depth of the Milky Way $X = m_H n_H h \approx 10^{-3} \text{ g/cm}^2$

\Rightarrow propagation of cosmic rays resembles a random-walk.

We can describe Cosmic Rays in the Milky Way as fluid!

Diffusion-equation



$n_i(E, \vec{r}, t)$ = electron density

$$= \frac{d^2 N}{dV dE}, dV = dx_1 dx_2 dx_3$$

$\Phi_E(E, \vec{r}, t)$ = energy flux per volume

$\Phi_{x_i}(E, \vec{r}, t)$ = spatial flux per energy interval

$Q(E, \vec{r}, t)$ = production rate of e^\pm per volume per energy interval

$$\begin{aligned}
\frac{\partial}{\partial t} n(E, \vec{r}, t) dE dV &= Q(E, \vec{r}, t) dE dV \\
&+ \left[\Phi_E(E, \vec{r}, t) - \left(\Phi_E(E, \vec{r}, t) + \frac{\partial \Phi_E}{\partial E} dE \right) \right] dV \\
&+ \sum_{i=1}^3 \left[\Phi_{x_i}(E, \vec{r}, t) - \left(\Phi_{x_i}(E, \vec{r}, t) + \frac{\partial \Phi_{x_i}}{\partial x_i} dx_i \right) \right] dE \frac{dV}{dx_i} \\
\Rightarrow \frac{\partial n}{\partial t} &= -\vec{\nabla} \cdot \vec{\Phi}_{\vec{r}} - \frac{\partial \Phi_E}{\partial E} + Q
\end{aligned}$$

Flux \sim gradient of the concentration $\Rightarrow \Phi_{x_i} = D_{ij} \frac{\partial n}{\partial x_j}$

$$\Rightarrow \frac{\partial n}{\partial t} = \vec{\nabla} \cdot (D \vec{\nabla} n) - \frac{\partial \Phi_E}{\partial E} + Q. \quad D = (D_{ij}) = \text{Diffusion tensor}$$

Loss rate due to energy loss mechanisms

$$-\frac{dE}{dt} \equiv b(E) \quad \Rightarrow \quad n(E) \frac{dE}{dt} = \Phi_E = -b(E)n(E)$$

Diffusion loss equation

$$\frac{\partial n}{\partial t} = \vec{\nabla} \cdot (D \vec{\nabla} n) + \frac{\partial}{\partial E} [b(E) n(E)] + Q(E)$$

Isotrope medium $\Rightarrow D = \text{Skalar, no spacial extension}$
 $\Rightarrow \vec{\nabla} \cdot (D \vec{\nabla} n) = D \vec{\nabla}^2 n$

Energy loss mechanisms for electrons

Energy loss rate $\frac{dE}{dt}$,

Cooling times $\tau = \frac{E}{(dE/dt)}$

Ionisation

Hydrogen $\left(-\frac{dE}{dt}\right)_{\text{ion}} = 7.64 \cdot 10^{-15} \left(\frac{n_H}{\text{m}^{-3}}\right) (3 \ln \gamma + 19.8) \text{eV s}^{-1}$

↑
relativistic rise (Bethe-Bloch)

Thus $\left(\frac{dE}{dt}\right) \approx 10^{-5} \left(\frac{n_H}{\text{m}^{-3}}\right) \text{eV Jahr}^{-1}$ and $\tau \sim E n_H^{-1}$

Bremsstrahlung (interaction with nuclei)

$$\text{Hydrogen} \quad \left(\frac{dE}{dt} \right)_{\text{brems}} = 3.66 \cdot 10^{-22} \left(\frac{n_H}{\text{m}^{-3}} \right) E \text{ s}^{-1}$$

$$\text{H-plasma} \quad \left(\frac{dE}{dt} \right)_{\text{brems}} = 7.0 \cdot 10^{-23} \left(\frac{n_H}{\text{m}^{-3}} \right) (\ln \gamma + 0.36) E \text{ s}^{-1}$$

$$\Rightarrow \tau \sim n_H^{-1}$$

Adiabatic losses

Adiabatic extension of a source (e.g. SNR)

$$dU = -p dV$$

(Expansion of a volume \rightarrow work \rightarrow loss of inner energy)

$$\text{e.g. homogenously expanding sphere} \quad \left(-\frac{dE}{dt} \right)_{\text{ad}} = \left(\frac{1}{R} \frac{dR}{dt} \right) E$$

$$\Rightarrow \tau \sim \text{const}$$

Synchrotron-radiation

Source: high energy electrons/positrons in B-field

Basics: Radiation in rest frame of the charge (Lamor Formula)

$$-\frac{dE}{dt} = \frac{q^2 |\ddot{\vec{r}}|^2}{6\pi\epsilon_0 c^3} \quad \left(\frac{dE}{dt} \text{ is lorentz-invariant} \right)$$

Dipol-radiation: $|\vec{E}| \sim |\sin \theta|$
 $I(\theta) \sim \sin^2 \theta$

Polarisation: $\vec{E} \parallel \vec{r}$ at large distance \perp diplo axis

Example: Motion in a constant B-field

$$v_{\perp} = v \sin \theta, \quad v_{\parallel} = v \cos \theta$$

Cyclotron-frequency $(\gamma m \dot{\vec{v}} = q \vec{v} \times \vec{B})$

$$\nu_g = \frac{1}{2\pi} \frac{qB}{\gamma m}$$

$$q = e, \quad m = m_e$$

$$\nu_g = 2.8 \gamma^{-1} \text{MHz} (B/1 \text{G}) \rightarrow \text{Radio}$$

$$|\vec{a}| = |\dot{\vec{v}}_{\perp}| = \frac{eB}{\gamma m_e} v \sin \alpha \quad \text{Zentripetal acceleration in B-System (Laboratory)}$$

$$|\vec{a}'| = \gamma^2 |\vec{a}| \quad \text{in current rest frame}$$

Lamor-Formula

$$-\frac{dE}{dt} = \frac{e^2 |\ddot{\vec{r}}|^2}{6\pi\epsilon_0 c^3} = s \underbrace{\left(\frac{e^4}{6\pi\epsilon_0^2 c^4 m_e^2} \right)}_{\sigma_T} \left(\frac{v}{c} \right)^2 c \underbrace{\left(\frac{B^2}{2\mu_0} \right)}_{U_{\text{mag}}} \gamma^2 \sin^2 \alpha$$

$$\sigma_T = \frac{e^4}{6\pi\epsilon_0^2 c^4 m_e^2}, \quad U_{\text{mag}} = \frac{B^2}{2\mu_0}, \quad \epsilon_0 \mu_0 = 1/c^2$$

$$\Rightarrow \boxed{\left(-\frac{dE}{dt} \right) = 2 \sigma_T c U_{\text{mag}} \left(\frac{v}{c} \right)^2 \gamma^2 \sin^2 \alpha}$$

Average over isotropical velocity distribution

$$\langle \sin^2 \alpha \rangle = \frac{1}{2} \int_{-1}^1 d \cos \alpha \sin^2 \alpha = \frac{1}{2} \int_{-1}^1 du (1 - u^2) = \frac{2}{3}$$

$$\left\langle -\frac{dE}{dt} \right\rangle = \frac{4}{3} \sigma_T c U_{\text{mag}} \left(\frac{v}{c} \right)^2 \gamma^2$$
$$= 1.058 \cdot 10^{-14} (B/\text{T})^2 \gamma^2 \beta^2 \text{ W}$$

for particles with an isotropical velocity distribution

$$\text{Cooling time } \tau_{\text{sy}} = \frac{3 m_e^2 c^3}{4 \sigma_T U_{\text{mag}} E} = 4 \cdot 10^{10} \left(\frac{B}{100 \mu \text{G}} \right)^{-2} \left(\frac{E}{1 \text{TeV}} \right)^{-1} \text{ s}$$

Cooling is more efficient for higher energies \Rightarrow steepening of the electron spectrum

Inverse Compton-effect

Compton effect

Kinematics

$$\frac{\Delta \lambda}{\lambda} = \epsilon (1 - \cos \alpha), \quad \epsilon = \frac{\hbar \omega}{m_e c^2}$$

Dynamics: Klein-Nishima

$$\sigma_{\text{KN}} = \frac{\pi r_e^2}{\epsilon} \left\{ \left[1 - \frac{2(\epsilon+1)}{\epsilon} \right] \ln(2\epsilon+1) + \frac{1}{2} + \frac{4}{\epsilon} - \frac{1}{2(2\epsilon+1)^2} \right\}$$
$$\approx \begin{cases} \sigma_T (1 - 2\epsilon) & \epsilon \ll 1 \text{ (Thomson-Grenzfall)} \\ \pi r_e^2 \frac{1}{\epsilon} \left(\ln(2\epsilon) + \frac{1}{2} \right) & \epsilon \gg 1 \text{ (ultrarelativistisch)} \end{cases}$$

Inverse Compton-effect

Energy loss rate of electrons

$U_{\text{rad}} \equiv$ energy density of the isotropical radiation field with $\gamma \hbar \omega \ll m_e c^2$

$$\left\langle -\frac{dE}{dt} \right\rangle = \frac{4}{3} \sigma_T c U_{\text{rad}} \left(\frac{v}{c}\right)^2 \gamma^2 \quad (\text{see sychrotron radiation})$$

Cooling time $\tau_{\text{sy}} = \frac{3 m_e^2 c^3}{4 \sigma_T U_{\text{rad}} E} = 4 \cdot 10^{13} \left(\frac{E}{1 \text{ TeV}}\right)^{-1} \text{ s}$ for $U_{\text{CMB}} = 0.25 \text{ eV/cm}^3$

Diffusion lost equation

$$\frac{\partial n}{\partial t} = \vec{\nabla} \cdot (D \vec{\nabla} n) + \frac{\partial}{\partial E} [b(E) n(E)] + Q(E)$$

How to solve?

- define source distribution
- define boundary conditions

Most simple example

- infinite, homogeneous source distribution
- Injection spectrum $Q(E) = K \cdot E^{-x}$
- steady state

$$\Rightarrow \frac{\partial n}{\partial t} = 0, \quad \vec{\nabla} n = \vec{0}$$

$$\Rightarrow \frac{d}{dE} [b(E)n(E)] = -Q(E)$$

$$\Rightarrow n(E) = -\frac{1}{b(E)} \cdot \frac{K}{1-x} E^{-x+1} + \underbrace{\text{const}}_{=0, \text{ because } \lim_{E \rightarrow \infty} n(E) = 0}$$

$$\Rightarrow n(E) = \frac{K}{x-1} \frac{E^{-(x-1)}}{b(E)}$$

Ansatz for $b(E) = -\frac{dE}{dt}$: (leading orders in E)

$$b(E) = \underbrace{A_1 \left(2 \ln \frac{E}{m_e c^2} + 19,8 \right)}_{\substack{\uparrow \\ \text{Ionisation}}} + \underbrace{A_2 E}_{\substack{\uparrow \\ \text{Bremsstrahlung} \\ (+\text{adiabatic losses})}} + \underbrace{A_3 E^2}_{\substack{\uparrow \\ \text{Synchrotron, I.C.}}}$$

Ionisation dominates

$$\Rightarrow n(E) \sim E^{-(x-1)} \sim E \cdot Q(E)$$

Bremsstrahlung dominates

$$\Rightarrow n(E) \sim E^{-x} \sim Q(E)$$

Synchrotron radiation + I.C. dominates $\Rightarrow n(E) \sim E^{-(x+1)} \sim \frac{Q(E)}{E}$

Simple description of the diffusion („Leaky box type“)

$\tau(E)$ = life time in „galactic confinement volume“

- $D = 0$ in confinement volume

- loss term = $\frac{n(E)}{\tau(E)}$

Comparison of cooling times

$$\underbrace{\tau_1 < \tau_2 \dots}_{\text{relevant energy}} \ll \tau(E) \ll \underbrace{\tau_k < \dots < \tau_n}_{\text{not relevant}}$$

relevant energy

loss mechanisms

→ steady state solution

without diffusion

not relevant

particles escape

before losing energy

Example

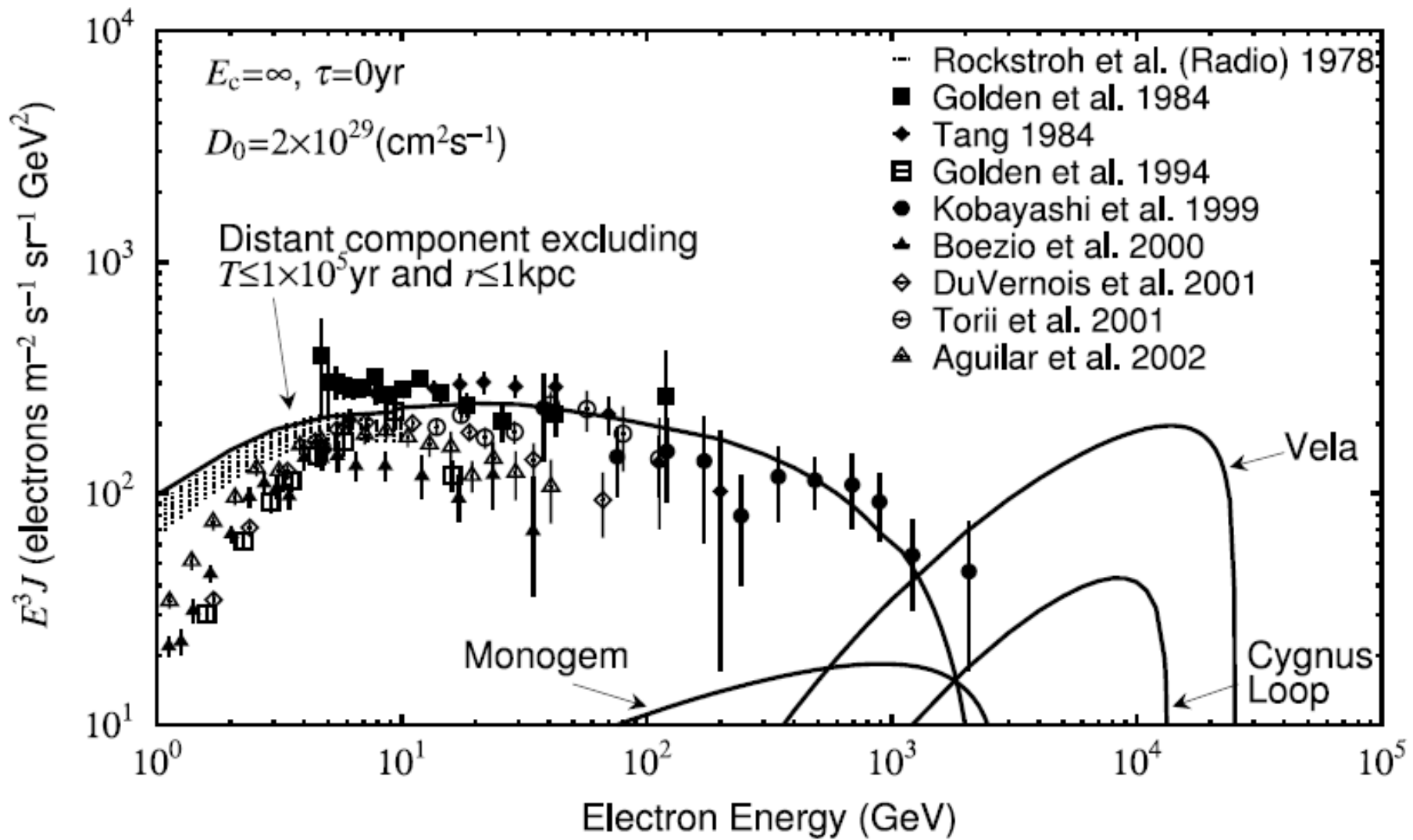
Typical for nuclei: $\tau \simeq (1 \dots 3) \cdot 10^7$ years

Assumption: τ similar for e^\pm

$E = 300 \text{ MeV}$, $n_H = 10^6 \text{ m}^{-3}$ $\rightarrow \tau_{\text{ionisation}} \simeq 3 \cdot 10^7$ Jahre
 \rightarrow Ionisation relevant for $E \leq 300 \text{ MeV}$
 $\rightarrow n(E) \sim E^{-(x-1)}$

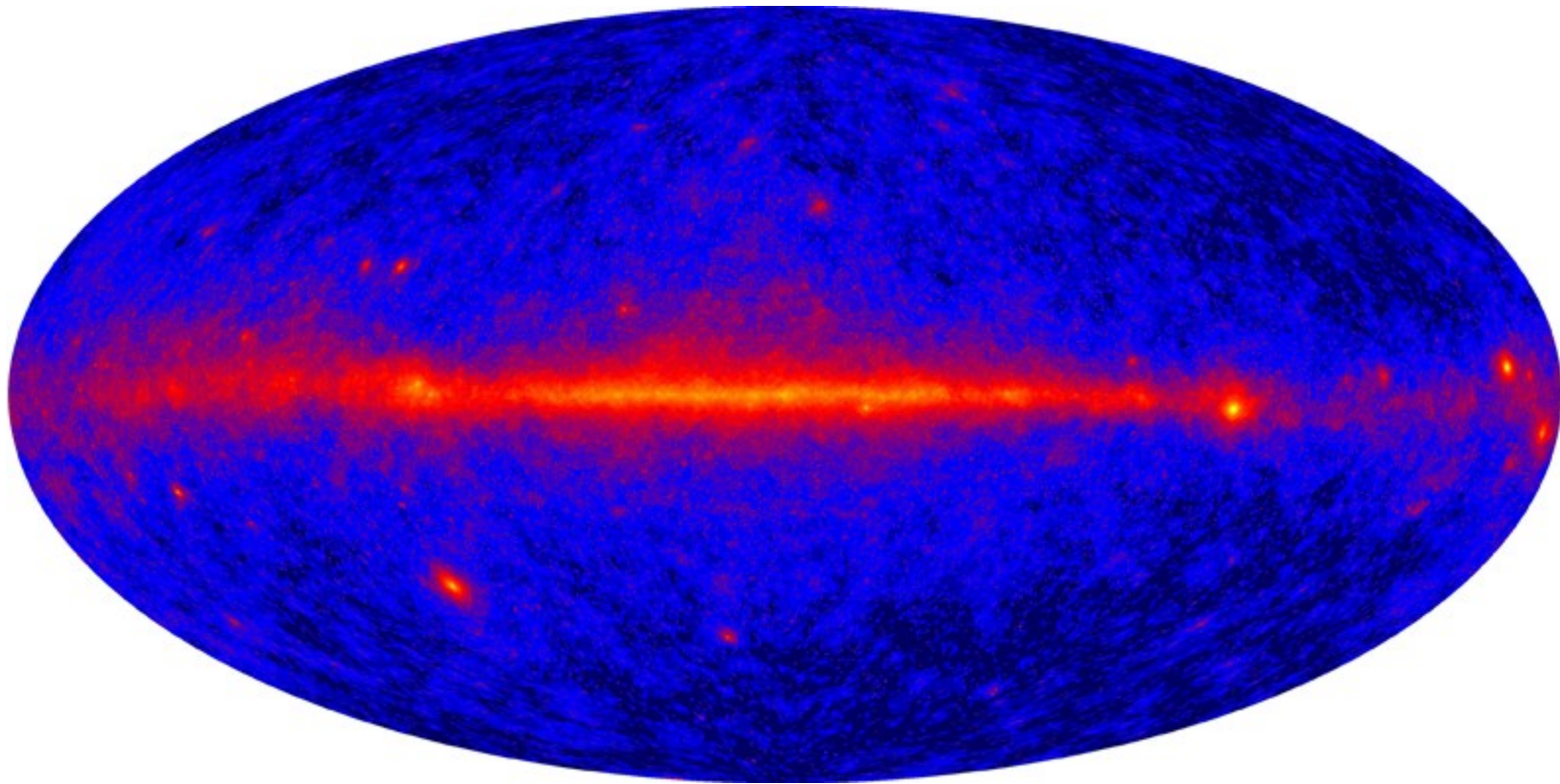
$E = 3 \text{ GeV}$, $n_H = 10^6 \text{ m}^{-3}$ $\rightarrow \tau_{\text{brems}} \simeq 5 \cdot 10^7$ Jahre
 \rightarrow Bremsstrahlung relevant around $E \simeq 1 \text{ GeV}$
 $\rightarrow n(E) \sim E^{-x}$

$E = 10 \text{ GeV}$, $B = 6 \cdot 10^{-10} \text{ T}$ $\rightarrow \tau_{\text{synchr}} \simeq 3 \cdot 10^5$ Jahre $\simeq O(\tau_{\text{IC}})$
 \rightarrow Synchr. + I.C. relevant for $E > 10 \text{ GeV}$
 $\rightarrow n(E) \sim E^{-(x+1)}$
 $\rightarrow O(100 \text{ pc})$



Diffusion of nuclei

Galactic gamma-rays



Direct measurement of the radiation power in the Milky Way $L_\gamma(E_\gamma > 100 \text{ MeV}) \approx 10^{32} \text{ W}$

Inelastic cross-section for $p \text{ Nuclei} \rightarrow X$

$$\sigma_{pp} \approx [31.5 + 0.46 \ln^2(E/50 \text{ GeV})] \text{ mb} \quad (1 \text{ mb} = 10^{-31} \text{ m}^2)$$

$$\sigma_{pA} / \sigma_{pp} \approx A^{2/3} (1.3 + 0.15 \log_{10} A) \quad (\text{good for } A > 7)$$

$$\text{Interaction probability} \quad P = \frac{N \sigma}{A} = n dl \sigma \stackrel{!}{=} \frac{dl}{\lambda}$$

$$\text{Interaction length} \quad \lambda = \frac{1}{n \sigma} \quad (n_H = 1 \dots 2 \cdot 10^6 \text{ 1/m}^3)$$

$$\text{Interaction rate} \quad \nu_{WW} = c / \lambda = \sigma n c$$

$$pp \rightarrow \pi^\pm, \pi^0, \dots$$

→ $\gamma\gamma$ dominant for γ -Spectrum for $E < 100 \text{ MeV}$

→ Neutrino source

$$\text{Isospinsymmetrie} \Rightarrow \approx \frac{2}{3} E \text{ in } \pi^\pm, \approx \frac{1}{3} E \text{ in } \pi^0 \quad (\rightarrow \gamma\gamma)$$

Test of the $\pi^0 \rightarrow \gamma\gamma$ hypothesis

$$L_\gamma \approx \nu_{WW}(pp) \cdot \sum_{i \text{ (CR in Galaxy)}} \frac{E_i}{3} = \frac{1}{3} \sigma_{pp} n_H c \epsilon_{CR} \cdot V_{\text{Galaxy}}$$

ϵ_{CR} = energy density of charged CR \approx protonen

$$\approx 10^6 \text{ eV m}^{-3}$$

$$n_H \approx 10^6 \text{ m}^{-3}$$

$$\sigma_{pp} \approx 32 \cdot 10^{-31} \text{ m}^2$$

$$V_{\text{Galaxy}} \approx 400 \text{ pc} \cdot \pi \cdot (8 \text{ kpc})^2 \approx 2 \cdot 10^{60} \text{ m}^3$$

$$\Rightarrow \boxed{L_{\pi \rightarrow \gamma\gamma} \approx 1.3 \cdot 10^{32} \text{ W}}$$

Measured

$$L_\gamma(E_\gamma > 100 \text{ MeV}) \approx 10^{32} \text{ W}$$

Diffusion equation for nuclei

$$\frac{\partial n_i}{\partial t} = \vec{\nabla} \cdot (D \vec{\nabla} n_i) + \frac{\partial}{\partial E} [b(E) n_i(E)] + Q(E) - \frac{n_i}{\tau_i} + \sum_j P_{ij} \frac{n_j}{\tau_j}$$

n_i = Number density of nuclei i

$\tau_i(E)$ = Lifetime for spallation from nuclei i

$P_{ij}(E)$ = Mean number of nuclei i per spallation from nuclei j
($P_{ij} \neq 0$ only for $A(\text{ nuclei } i) < A(\text{ nuclei } j)$)

Simple approximation for light nuclei in isotropic medium

- diffusion small compared to spallation loss $\Rightarrow D \approx 0$
- $m_{\text{nuclei}} \gg m_e \Rightarrow n$ no energy losses $\Rightarrow b(E) \approx 0$
- light nuclei: Li, Be, B rare $\Rightarrow Q_i(E) \approx 0$

Where are we – a short summary

- Cosmic rays are messengers from the high energy Universe
- The cosmic rays we measure on Earth are typical for the cosmic rays population in our Milky Way
- Cosmic-ray propagation can be described by a diffusion equation, i.e. cosmic rays behave like a fluid in a box
- Next steps (today)
 - Age of cosmic rays → sources must be active now
 - Energy dependent propagation → source spectra are power laws $dn/dE \sim E^{-2}$
 - Acceleration of cosmic rays
 - Source detection?

Simplest assumption

All CR have the same fixed age ξ after injection when observed on Earth

$$\Rightarrow \Rightarrow \frac{dn_i}{d\xi} = -\frac{n_i(\xi)}{\xi_i} + \sum_j P_{ij} \frac{n_j(\xi)}{\xi_j} \quad \text{with } n(\xi) \text{ observed on Earth}$$

L-Kerne (L = light): Li, Be, B; $n_L(0)=0$ Injection time (there are no sources

M-Kerne (M = medium): C, N, O most abundant primary nuclei, $n_M(0) \neq 0$

Fragmentationswahrscheinlichkeit

$$\begin{array}{l} \text{Spallation } M \rightarrow L, M \quad P_{ML} \approx \overbrace{0.28} \\ L \rightarrow M, L \quad P_{LM} = P_{LL} = 0 \end{array} \quad P_{MM} = 0$$

$$\frac{dn_M}{d\xi} = -\frac{n_M(\xi)}{\xi_M} \quad \text{no refill}$$

$$\frac{dn_L}{d\xi} = -\frac{n_L(\xi)}{\xi_L} + \frac{P_{ML}}{\xi_M} n_M(\xi)$$

$$\text{X-section } \Rightarrow \quad \xi_M \approx 60 \text{ kg/m}^2, \quad \xi_L \approx 84 \text{ kg/m}^2 \quad (\text{from known X-sections})$$

Age of Cosmic Rays

Estimate of the confinement volume

$$\xi = \bar{\rho} c \tau \quad \text{with} \quad \bar{\rho} = \text{mean density}, \xi = 48 \text{ kg/m}^2 \Rightarrow \tau = 3 \cdot 10^6 \text{ years}$$

Extension of a galaxy 1-10 kpc \Rightarrow escape after $3 \cdot 10^3 - 3 \cdot 10^4$ years

\Rightarrow confinement volume

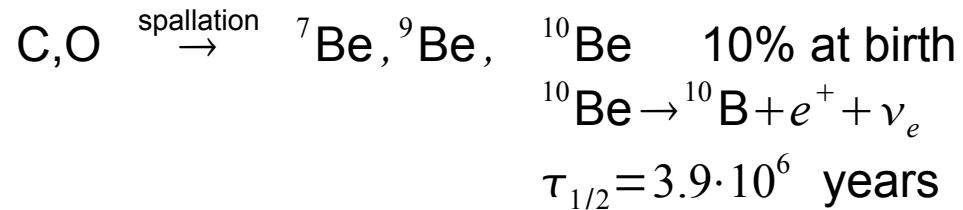
Improved estimate of the age (confinement time):

Measure radioactive isotopes, half life time $\tau_{1/2}$

$$\Rightarrow \text{additional loss term: } \frac{u_i}{\tau_{\text{dec}}(i)}$$

$$\tau_{\text{dec}}(i) = \gamma_i \tau_{1/2} / \ln 2, \quad \gamma_i \Leftrightarrow \text{time dilatation}$$

Example



Measurement

$$n({}^{10}\text{Be})/n({}^7\text{Be}), \quad n({}^{10}\text{Be})/n({}^9\text{Be}) \Rightarrow \text{only } 28\% \text{ } {}^{10}\text{Be}$$
$$\Rightarrow \text{mean age at arrival on Earth} = O(10^7) \text{ Jahre}$$

Simplified model

Leaky Box:

- $D=0$
- loss term = $-\frac{n_i}{\tau_e(i)}$ τ_e = local escape time in galaxy

Steady state:

- $\dot{n}_i=0$
- no source terms $Q_i=0$, Be produce alone in spallation of C,O,N
- no energy loss $b(E)=0$

$$\Rightarrow 0 = -\frac{n_i}{\tau_e(i)} - \frac{n_i}{\tau_{\text{Spal}(i)}} + \underbrace{\sum_{j \in \{C, N, O\}} \frac{P_{ij}}{\tau_{\text{Spal}(j)}} n_j}_{C_i}$$

for $i \in \{^7\text{Be}, ^9\text{Be}\}$

and

$$0 = -\frac{n_k}{\tau_e(k)} - \frac{n_k}{\tau_{\text{Spal}(k)}} + C_k - \frac{n_k}{\tau_{\text{dec}}(k)}$$

für $k = ^{10}\text{Be}$

$$\Rightarrow \frac{n_k}{n_i} = \frac{C_k}{C_i} \frac{1/\tau_e(i) + 1/\tau_{\text{Spal}(i)}}{1/\tau_e(k) + 1/\tau_{\text{Spal}(k)} + 1/\tau_{\text{dec}}(k)}$$

Measurement of $\frac{n_k}{n_i} \Rightarrow \tau_e \approx 10^7$ years

with $\xi = 48 \text{ kg/m}^3$

$\Rightarrow \rho_{\text{IS}} \approx 3 \cdot 10^5 \text{ m}^3$

Die GZK Grenze

Magnetische Einschlussgebiete \leftrightarrow Gyroradius

$$r = R_B \frac{\sin \theta}{Bc}, \quad R_B = \frac{pc}{Ze}$$

Galaktisch: $B \approx 3 \cdot 10^{-10} \text{ T}$

Protonen

- $E \approx 10^{15} \text{ eV} \rightarrow r \leq 0.36 \text{ pc}$
 \approx Skala der Diffusionsgleichung
 \Rightarrow Isotropie
- $E > 10^{15} \text{ eV} \rightarrow$ Anisotropie steigt, Entweichzeit sinkt, Diffusion verliert an Relevanz
- $E \approx 10^{18} \text{ eV} \rightarrow r \leq 3.6 \text{ kpc} \approx$ Halo-Radius
- $E \approx 10^{21} \text{ eV} \rightarrow$ nicht galaktisch eingeschlossen
 $B \approx 3 \cdot 10^{-12} \text{ T} \Rightarrow r \leq 36 \text{ Mpc} \Rightarrow$ lokale Gruppe

Dominante Verlustprozesse höchstenergetischer Strahlung

Kollisionen mit CMB (+IR, V, ...) \Rightarrow Photoproduktion

a) Schwelle

$$p + \gamma_{\text{CMB}} \rightarrow \begin{cases} n\pi^+ \\ p\pi^0 (\rightarrow \gamma\gamma) \end{cases}$$

$$\sqrt{s} \geq (m_p + m_\pi) c^2 \approx 1.1 \text{ GeV}$$

Labor

$$\sqrt{s} \approx \sqrt{2 p_p p_\gamma} \approx \sqrt{2 E_p E_\gamma (1 + \cos \theta)} \approx \sqrt{2 E_p E_\gamma}$$

$$\Rightarrow E_p \approx \frac{s}{2 E_\gamma} \geq \frac{(1.1 \text{ GeV})^2}{2 E_\gamma}$$

Planck-Spektrum für $T \approx 2.73 \text{ K} \Rightarrow \boxed{E_p \geq 5 \cdot 10^{19} \text{ eV}}$

b) Erste Resonanz \Rightarrow GZK-Cut-Off (Greisen, Za....)

$$p \gamma_{\text{CMB}} \rightarrow \Delta^+ \rightarrow \begin{cases} n\pi^+ & 33.3\% \\ \pi^0 p & 66.7\% \end{cases}$$

$$(\uparrow\uparrow\downarrow) J^P = \left(\frac{1}{2}\right)^+ \quad (\uparrow\uparrow\uparrow) J^P = \left(\frac{3}{2}\right)^+$$

$$L=0 \quad L=0$$

$$m_p = 938 \text{ MeV}/c^2 \quad m_\Delta = 1232 \text{ MeV}/c^2$$

Schwelle

$$\sigma_{\gamma p} \approx 0.1 \text{ mb} \rightarrow \text{Resonanz } \sigma_{\gamma p} \approx 0.6 \text{ mb}$$

Resonanzlage

$$\sqrt{s} = m_\Delta c^2, \quad E_p \geq \frac{(m_\Delta c^2)^2}{2 E_\gamma} \xrightarrow{T=2.73\text{K}} E_p > 6 \cdot 10^{19} \text{ eV}$$

Reichweite

$$\begin{aligned}\lambda &= (\sigma_{\gamma p} n_{\gamma})^{-1} \\ n_{\gamma} &\approx 5 \cdot 10^8 \text{ m}^{-3}, \quad \langle \sigma_{\gamma p} \rangle \approx 0.75 \text{ mb} \\ \Rightarrow \lambda &\approx 3 \text{ Mpc}, \quad \tau_{\text{propagation}} \approx 10^7 \text{ Jahre}\end{aligned}$$

- Höchstenergetische Protonen ($>10^{20}$ eV) stammen aus lokaler Gruppe \rightarrow Abfall des Spektrums (GZK Cut-Off)
- Beobachtung “Knöchel”, d.h. Ausflachung, Widerspruch?
(Spektrum Auger, Skymap Auger)
- Beschleunigung in AGN?
- Exotische Alternative: Primordiale schwere Teilchen, $m > 10^{20} \text{ eV}/c^2$
- das wird in den nächsten Jahren noch sehr spannend!!!!

Z